

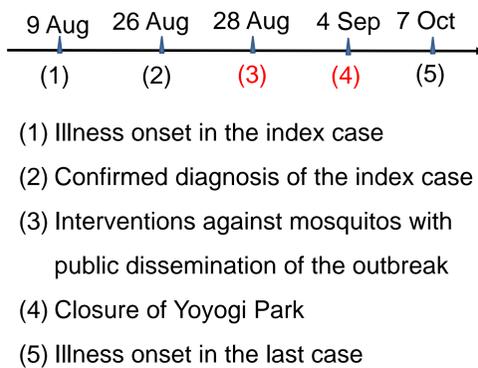
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Introduction

In summer 2014, an autochthonous outbreak of dengue occurred in Tokyo, in which Yoyogi Park acted as the focal area of transmission[1]. Recognizing the outbreak, concerted efforts were made to control viral spread, which included mosquito control, public announcement of the outbreak, and a total ban on entering the park.

- Purpose:** (1) estimate the generation time and the effective reproduction number;
(2) assess the effectiveness of control measures.



Data

The reported cases were classified into:

- (i) Group 1: complete observation;
- (ii) Group 2: interval-censored observation;
- (iii) Group 3: missing observation of exposure.

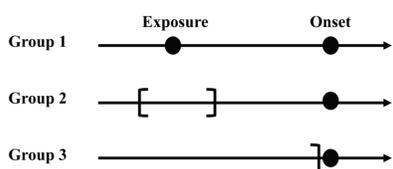


Fig 1. Illustrated time of exposure and classification of cases

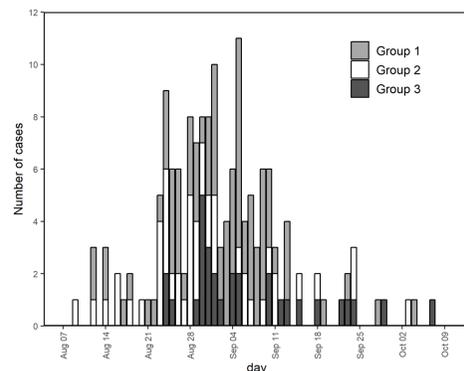


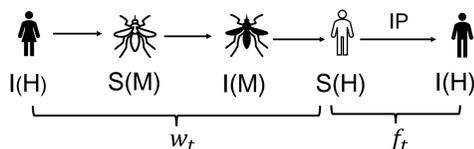
Fig 2. Temporal distribution of dengue by three classification groups of datasets

Group 1: 79; Group 2: 47; Group 3: 30

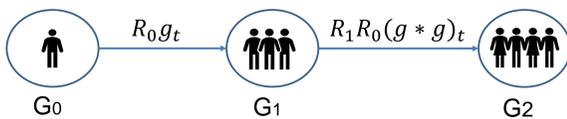
Model

Epidemic curve as the probability distribution

- Generation time: $g_t = \sum_{\tau=0}^t f_{t-\tau} w_{\tau}$.



- Generation-dependent model[2]



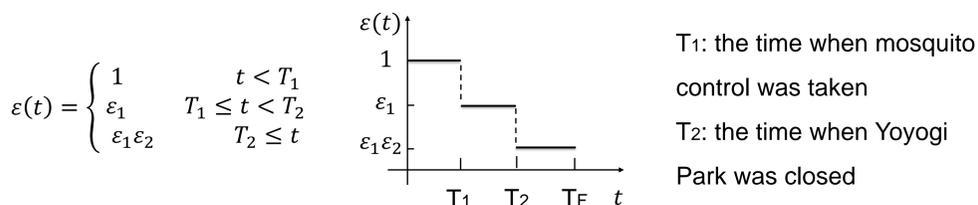
The epidemic curve of infection as the probability distribution **without interventions** (up to the fourth generation (G4)):

$$h(t) = \frac{g_t + R_1(g * g)_t + R_2 R_1(g * g * g)_t + R_3 R_2 R_1(g * g * g * g)_t}{1 + R_1 + R_2 R_1 + R_3 R_2 R_1}$$

where R_n is the reproduction number of $n+1$ generation infections.

Effectiveness of interventions

The relative reduction in reproduction number, $\varepsilon(t)$:



- The probability density of the epidemic curve of infection **with interventions**

$$u(t) = \frac{h(t)\varepsilon(t)}{\sum_{\tau=0}^t h(\tau)\varepsilon(\tau)}$$

- The effective reproductive number $R(t) = \frac{u_t}{\sum_{\tau=0}^t u_{t-\tau} g_{\tau}}$

Likelihood function

Group 1, $L_i^1(\theta_n; t_i^e, t_i^s, d_0) = u_z(t_i^e, d_0) f_{t_i^s - t_i^e}$

Group 2, $L_j^2(\theta_n; E_j^L, E_j^R, t_j^s, d_0) = \sum_{\tau=E_j^L}^{E_j^R} u_z(\tau, d_0) f_{t_j^s - \tau}$

Group 3, $L_k^3(\theta_n; t_k^s, d_0) = \sum_{\tau=t_0}^{t_k^s} u_z(\tau, d_0) f_{t_k^s - \tau}$

Maximum likelihood estimation (MSE)

Incubation period,

$$L^{IP}(\mu_{IP}, \sigma_{IP}; t^e, t^s) = \prod_{i=1}^{n_1} f_{t_i^s - t_i^e}$$

Total likelihood function,

$$L(\theta_n; t^e, t^s, E^L, E^R, d_0) = \prod_{i=1}^{n_1} L_i^1 \prod_{j=1}^{n_2} L_j^2 \prod_{k=1}^{n_3} L_k^3 \prod_{i=1}^{n_1} L_i^{IP}$$

Results

- **Parameter estimation**

Estimated incubation period

Mean: 5.8 (5.5, 6.0) days

Deviation: 1.8 (1.6, 2.1) days

Estimated mean generation time

12- 17 days

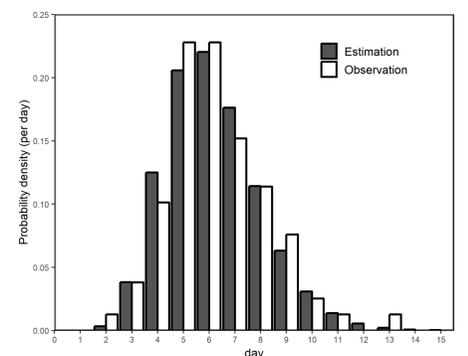


Fig 3. Probability distribution of incubation period

- **Model fitting with variable number of generations**

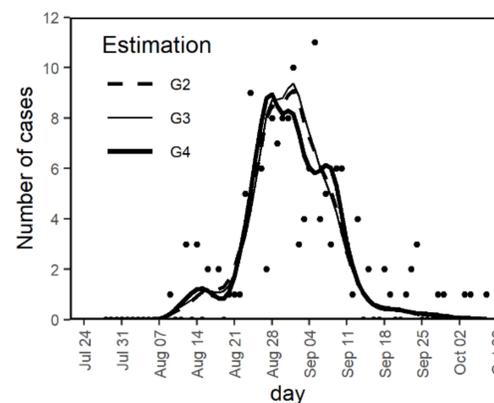


Fig 4. Comparison between observed and estimated epidemic curves with variable number of generation

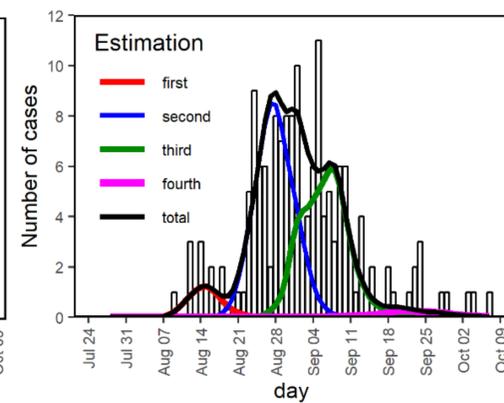


Fig 5. Comparison between observed and estimated epidemic curves with four generations

- **Effective reproduction number with variable number of generations**

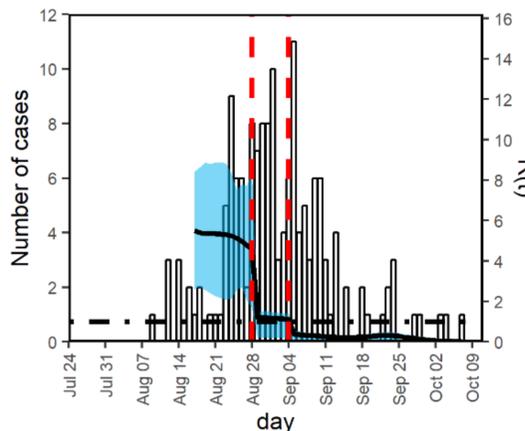


Fig 6. Estimated curve of the effective reproduction number with four generations

Generation-dependent reproduction number (R_n):

R_0 : 4.0 R_1 : 5.4 (2.7, 10.5)

R_2 : 4.3 (1.1, 16.8) R_3 : 0.4 (0.2, 1.0)

Estimated $\varepsilon(t)$:

ε_1 : 30%~70%; ε_2 : 40%~80%

Combined effect:

The relative reduction in transmission rate due to combined interventions $\varepsilon_1 \varepsilon_2$: 44%~88%.

Discussion

- A generation-dependent model was developed to parameterize the incidence of infection by convoluting the incidence of infection with the incubation period
- To fully halt virus transmission, the combined effect of mosquito control, public awareness campaigns, and park closure was needed for a substantial reduction in R_t

[1] Bureau of Social Welfare and Public Health, Tokyo Metropolitan Government. 2014.

[2] Akhmetzhanov AR, et al. PLoS Curr. 2018; 10.