Yield failure of the subducting plate at the Mariana Trench

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A R T I C L E   I N F O
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Mariana trench
3-D plate bending
Numerical simulation
Yield zone depth
Earthquakes

A B S T R A C T
Two tectonic plates converge at subduction zones where the subducting plate bends. Flexural bending of a subducting plate at a trench results in pervasive normal faulting, providing conduits for plate hydration and influencing the water budget and seismic behavior of the plate interface. 2-D plate bending simulations have demonstrated high strains due to strong bending may result in loss of strength of the lithosphere and intraplate earthquakes near the trench axis. However 3-D plate bending deformation may affect the along-strike slab pull force, especially when the deflection changes along the trench. Here we simulated the 3-D plate bending deformation and calculated bending stresses, and brittle failure of the Pacific plate at the Mariana Trench. We find that both the plate deflection and the yield zone depth (~16–20 km) increases from the northern to southern Mariana Trench. The water flux in the plate at the southern Mariana Trench is estimated to be about 15% greater than that of the northern Mariana Trench. By comparing with 2-D models, we further find that the 2-D approaches may underestimate the yield zone depth as they ignored the along-trench effects of plate deflection. The new results provide a self-consistent framework for interpretation of the observed surface normal faults, extensional earthquakes, and the inferred hydration of the subducting plate as constrained by seismic velocity anomalies.

1. Introduction

Flexural bending causes extensional brittle failure at the shallow part of a subducting plate (Watts, 2001). The resulting normal faulting can provide pathways for seawater to hydrate the crust and upper mantle prior to subduction (Ranero and Sallares, 2004; Rupke et al., 2004; Grevemeyer et al., 2007), thus their pervasiveness and depth extent strongly affect the water budget of a subducting plate (Faccenda et al., 2009). The hydration in turn influences the seismic behavior of the subduction plate interface (Ammon et al., 2008; Beaven et al., 2010; Grevemeyer et al., 2007), providing conduits for plate hydration and influencing the water budget and seismic behavior of the plate interface. 2-D plate bending simulations have demonstrated high strains due to strong bending may result in loss of strength of the lithosphere and intraplate earthquakes near the trench axis. However 3-D plate bending deformation may affect the along-strike slab pull force, especially when the deflection changes along the trench. Here we simulated the 3-D plate bending deformation and calculated bending stresses, and brittle failure of the Pacific plate at the Mariana Trench. We find that both the plate deflection and the yield zone depth (~16–20 km) increases from the northern to southern Mariana Trench. The water flux in the plate at the southern Mariana Trench is estimated to be about 15% greater than that of the northern Mariana Trench. By comparing with 2-D models, we further find that the 2-D approaches may underestimate the yield zone depth as they ignored the along-trench effects of plate deflection. The new results provide a self-consistent framework for interpretation of the observed surface normal faults, extensional earthquakes, and the inferred hydration of the subducting plate as constrained by seismic velocity anomalies.

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varies significantly from south to north (Ryan et al., 2009; Weatherall et al., 2015) (Fig. 1a and Fig. S1a in the Supplementary material); (2) the age range of the Mariana subducting plate is relatively narrow (140–160 Ma), and thus the variation in the effective elastic plate thickness is not a first-order effect; (3) the Mariana Trench has been the focus of recent multiple seismic experiments (Cai et al., 2018; Wan et al., 2019); and (4) high-resolution bathymetry data are available for most of the Mariana Trench, providing direct constraints on the spatial variations in surface normal faults.

In this study, we developed one of the first 3-D bending analyses of the Pacific plate at the Mariana Trench. We first used a thin-plate approximation to model the vertical deformation of a 3-D elastic plate and then analyzed the depth variation in the extensional stresses and yielding of the plate. The calculated plate deformation was then compared with the observed surface normal faults and extensional earthquakes. Finally, we estimated the water flux and degree of serpentinization in the subducting Pacific plate, comparing the results with the shear-wave seismic velocity profiles. Together, these analyses provide new insights on the 3-D processes of a subducting plate.

2. Method

2.1. Flexural model and curvature calculation

We used the Kirchhoff-Love thin plate assumption (Timoshenko and Woinowsky-Krieger, 1959) to calculate the vertical deformation (w) of a 3-D thin plate (Wessel, 1996):

\[
\nabla^2 (D \nabla^2 w) - (1 - v) \times \left( \frac{\partial^2 D}{\partial x^2} \frac{\partial^2 w}{\partial x^2} + 2 \frac{\partial^2 D}{\partial x \partial y} \frac{\partial^2 w}{\partial x \partial y} + \frac{\partial^2 D}{\partial y^2} \frac{\partial^2 w}{\partial y^2} \right) - N_{xx} \frac{\partial^2 w}{\partial x^2} - 2N_{xy} \frac{\partial^2 w}{\partial x \partial y} + N_{yy} \frac{\partial^2 w}{\partial y^2} + \Delta \rho g w = q(x, y)
\]

(1)

where \(q(x, y)\) is spatially varying vertical loading force; \(\Delta \rho = \rho_m - \rho_w\) is the density contrast between the mantle and water; and \(g\) is the gravitational acceleration. \(N_{xx}, N_{xy},\) and \(N_{yy}\) are the in-plane forces. The flexural rigidity \(D\) is given by \(D = \frac{Et_e^3}{12(1 - v^2)}\), where \(E\) and \(v\) represent the Young's modulus and Poisson's ratio, and \(T_e\) is the effective elastic thickness (Table 1). Unlike 2-D model in which the bending moment (\(M\)) and vertical shear stress (\(V\)) have simple forms, \(M\) and \(V\) in 3-D situation are given by:

\[
\begin{align*}
M_x &= -D \left( \frac{\partial^2 w}{\partial x^2} + \nu \frac{\partial^2 w}{\partial y^2} \right) \\
M_y &= -D \left( \frac{\partial^2 w}{\partial y^2} + \nu \frac{\partial^2 w}{\partial x^2} \right) \\
M_{xy} &= -D (1 - \nu) \frac{\partial^2 w}{\partial x \partial y}
\end{align*}
\]

(2)

and

Fig. 1. (a) Topography of the Mariana Trench. The shaded area is the modeled subducting plate. The black arrows represent the subduction directions. The blue beach balls show the outer-rise extensional earthquakes of \(Mw \geq 4.0\) recorded by the GCMT database. (b) Model setup. The grid size of the model is \(\sim 6.5\) km, yielding a total of 246×383 grids. Red line marks the trench axis, which is subjected to a boundary loading \(q(x, y)\) along the trench axis. Blue and purple color mark the areas with \(T_e^M(x, y)\) and \(T_e^m(x, y)\), respectively. Black dashed line indicates the breaking points between the \(T_e^M\) and \(T_e^m\). Blue color marks the study area. The boundary \(\Gamma_1\) is free boundary, while \(\Gamma_2, \Gamma_3,\) and \(\Gamma_4\) are fixed.
Previous studies used trench-axis loading in the form of bending analysis and not of interest. Therefore, we only analyzed the line) to the west of the trench axis. Note that only the region east of the

\[ \Gamma \]

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>( E )</td>
<td>Young's modulus</td>
<td>( 7 \times 10^{10} )</td>
<td>Pa</td>
</tr>
<tr>
<td>( \dot{g} )</td>
<td>Acceleration due to gravity</td>
<td>9.81</td>
<td>m/s(^2)</td>
</tr>
<tr>
<td>( \nu )</td>
<td>Poisson’s ratio</td>
<td>0.25</td>
<td></td>
</tr>
<tr>
<td>( \mu_n )</td>
<td>Mantle density</td>
<td>3300</td>
<td>kg/m(^3)</td>
</tr>
<tr>
<td>( \nu_L )</td>
<td>Crust density</td>
<td>2700</td>
<td>kg/m(^3)</td>
</tr>
<tr>
<td>( \rho_s )</td>
<td>Sediment density</td>
<td>2000</td>
<td>kg/m(^3)</td>
</tr>
<tr>
<td>( \rho_w )</td>
<td>Water density</td>
<td>1030</td>
<td>kg/m(^3)</td>
</tr>
<tr>
<td>( C_0 )</td>
<td>Cohesion</td>
<td>44</td>
<td>MPa</td>
</tr>
<tr>
<td>( A )</td>
<td>Pre-exponential</td>
<td>( 1.4 \times 10^{-7} )</td>
<td>s(^{-1}) MPa(^n)</td>
</tr>
<tr>
<td>( n )</td>
<td>Stress exponent</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>( H_0^\sigma )</td>
<td>Zero-stress activation enthalpy</td>
<td>320</td>
<td>kJ mol(^{-1})</td>
</tr>
<tr>
<td>( \sigma_p )</td>
<td>Peiers stress or glide resistance</td>
<td>5.9</td>
<td>GPa</td>
</tr>
<tr>
<td>( p,q )</td>
<td>Geometry dependent parameters</td>
<td>( \frac{%}{1} )</td>
<td></td>
</tr>
<tr>
<td>( B )</td>
<td>A material-dependent parameter</td>
<td>( 1.10 \times 10^{-7} )</td>
<td>MPa(^{-n})</td>
</tr>
<tr>
<td>( E^p )</td>
<td>Activation energy</td>
<td>530</td>
<td>kJ mol(^{-1})</td>
</tr>
<tr>
<td>( V^p )</td>
<td>Activation volume</td>
<td>( 14 \times 10^{-6} )</td>
<td>m(^3) mol(^{-1})</td>
</tr>
</tbody>
</table>

The equation (1) was solved by the finite-difference method (FDM) under different boundary conditions and surface loading \( q(x, y) \) (Fig. 1b). The model parameters are displayed in Table 1. The boundary conditions include following: stress free on the boundary \( \Gamma_1 \), while \( \Gamma_2 \), \( \Gamma_3 \) and \( \Gamma_4 \) are fixed. They are given by:

\[ \begin{align*}
\Gamma_1: & \quad M = 0, V = 0, \\
\Gamma_2: & \quad w = 0, M = 0, \\
\Gamma_3: & \quad w = 0, M = 0, \\
\Gamma_4: & \quad w = 0, M = 0.
\end{align*} \]

In this study, we used a more generic boundary loading form \( q \), which represents synthetic loading and can adequately reproduce \( M_0 \) and \( V_0 \) numerically (Fig. S2 in the Supplementary material). Some previous studies suggested that \( T_z \) varies with plate age (Hunter and Watts, 2016; Zhang et al., 2018b), while other studies indicate little age dependence (Bry and White, 2007; Contreras-Reyes and Osses, 2010; Craig and Copley, 2014). In this study, for simplicity the \( T_z \) was divided into two parts: \( T_z^0 \) and \( T_z^e \) seaward and trench-ward of the outer rise, respectively, breaking at a distance of \( X_2 \) parallel to the trench axis (Fig. 1b). \( T_z^0 = 50 \) km was set to be a constant (Zhang et al., 2014). The \( q(x, y) \) and \( T_z^\sigma(x, y) \) vary freely along the trench axis. In order to avoid the potential edge effect of direct application of loading on the trench axis, the \( q(x, y) \) was applied at a constant distance of 60 km (green dashed line) to the west of the trench axis. Note that only the region east of the trench axis (purple and green colors) is of physical meaning and of interest, while the region west of the trench axis (gray area) is fictitious in the bending analysis and not of interest. Therefore, we only analyzed the predicted bending deformation in the study region (Fig. 1b). The grid size is \( \approx 6.5 \) km.

We aim to find a solution of combination of \( q, T_z^0, X_2 \) to minimize the root mean square (RMS) difference \( W_{\text{RMS}} \) between the modeled deformation and the non-isostatic topography:

\[ W_{\text{RMS}} = \sqrt{\frac{1}{n} \sum_{i=0}^{n} (w_i - \hat{w}_i)^2} \]

where \( n \) is the number of points of study area \( w^{\text{obs}} \) is the observation bathymetry data and \( w^0 \) is the calculated result using eq. (1). First, we used the previous 2-D thin plate model results (Zhang et al., 2014) to constrain the range of solution space of \( (q, T_z^0, X_2) \). Then we explored the solution space manually to seek solutions that are successively close to the observation until a deformation surface was obtained, which can capture the key features of the non-isostatic topography.

2.2. Calculation of extensional yield zone

Flexural bending of a subducting plate is expected to cause brittle yielding and plastic deformation in the upper and lower plates, respectively (Fig. 2a) based on the yield strength envelope (YSE) (Fig. 2c) (Byerlee, 1978; Garcia-Castellanos et al., 2000; Hunter and Watts, 2016). The maximum sustainable deviatoric stress at the upper plate was determined by the cohesion of the lithosphere \( C_0 \) (Fig. 2c, Table 1) (Lavier et al., 2000) and the maximum shear stress \( \Delta \sigma = \mu (\sigma_p - P_f) \) where \( \mu, \sigma_p \), and \( P_f \) are the rock frictional coefficient, normal stress, and pore fluid pressure on the fault planes, respectively. Plastic deformation at the lower plate is controlled by the temperature-dependent power-law rheology (Goetze, 1978; Goetz and Evans, 1979; Hirth and Kohlstedt, 2003; Mei et al., 2010; Hunter and Watts, 2016; Zhang et al., 2018a). In the ductile regime, combination of two ductile flow laws is adopted in our work (same as in Hunter and Watts, 2016). In the low-temperature regime, the ductile flow of low-temperature plasticity (LTP) is given by:

\[ \dot{\epsilon} = A \sigma^p \left( \frac{H^\sigma \dot{\epsilon}}{RT} \right) \left( 1 - \left( \frac{\sigma}{\sigma_p} \right)^n \right) \]

where \( \dot{\epsilon}, \sigma, R, T \) are the strain rate, differential stress, gas constant, and temperature, respectively. \( A \) is the pre-exponential determined by pressure, grain size, and volatile content. \( H^\sigma \) is the zero-stress activation enthalpy, \( n \) is a non-dimensional parameter and \( \sigma_p \) is the Peiers stress or glide resistance. \( p \) and \( q \) are geometry dependent parameters. The values of parameters in this study follow the work of Mei et al. (2010): \( A = 1.4 \times 10^{-7} \) s\(^{-1}\) MPa\(^n\), \( n = 2 \), \( H^\sigma = 320 \) kJ mol\(^{-1}\), \( \sigma_p = 5.9 \) GPa, \( p = 0.5 \), and \( q = 1 \). The temperature structure is shown in Fig. 2b (Stein and Stein, 1992). At higher temperature (\( -600-800 \) °C), the ductile flow of power-law creep (PLC) is given by:

\[ \dot{\epsilon} = B \epsilon^{\epsilon} \left( \frac{E^p + PV^e}{RT} \right) \]

where \( B \) is a material-dependent parameter, \( \epsilon \) is the stress exponent and \( E^p \) is the activation energy, \( V^e \) is the activation volume, \( P \) and \( T \) are pressure and temperature, respectively. The values of parameters in this study follow the work of Hirth and Kohlstedt (2003): \( B = 1.10 \times 10^{18} \) s\(^{-1}\) MPa\(^n\), \( E^p = 530 \) kJ mol\(^{-1}\), and \( V^e = 14.10 \times 10^{-6} \) m\(^3\) mol\(^{-1}\).

Following the work of Hunter and Watts (2016), we adopted the low-temperature rheology law of Mei et al. (2010) and the high-temperature rheology law of Hirth and Kohlstedt (2003), respectively. At the central depth, an elastic core is sandwiched between the upper brittle yield zone and the lower layer of plastic deformation (Fig. 2a). The deviatoric stress (Fig. 2c) in the elastic core was calculated by \( \Delta \sigma_{\epsilon}^{\text{elastic}} = \frac{E^p + PV^e}{k} \), where \( z \) presents the distance from the neutral plane, \( x_0 \) is the depth of the neutral plane, and \( k \) is the maximum plate deformation curvature which is the function of \( (x, y) \) in 3-D situation (Please see the section 2.3). The brittle yield zone was then determined by the maximum sustainable deviatoric stress and curvature of the flexural bending plate. Additional details of the calculation methods were described in Zhang et al., 2020a; Zhang et al., 2020b. All parameters used in flexural analysis are displayed in the Table 1.
2.3. Maximum curvature of plane

For 2-D models, the deviatoric stress can be calculated from the curvature along the profile (Please see the Section 2.2), while in the 3-D situation, the deviatoric stress should be calculated from the maximum curvature of plane (Garcia et al., 2019). According to the theory of differential geometry, the two principal curvatures at a given point on a surface measure how a surface bends in different directions at that point. If a surface $w(x, y)$ has continuous second-order partial derivatives, it could be described by the first and second fundamental forms of the surface:

$$S_1 = E_d x^2 + 2F_d x dy + G_d y^2$$

$$S_2 = L_d x^2 + 2M_d x dy + N_d y^2$$

where $E_d$, $F_d$, and $G_d$ are first basic parameters and $L_d$, $M_d$, and $N_d$ are second basic parameters. The normal curvature of any point $(u, v)$ on a surface is given by

$$k_n = \frac{S_2}{S_1} = \frac{L_d du^2 + N_d dv^2}{E_d du^2 + G_d dv^2}$$

Assuming that $k_1$ and $k_2$ are the maximum and minimum of the normal curvature $k$, they can be described by

$$(F_0^p G_0^p)^2 k_1^2 - (L_0 G_0 - 2M_0 F_0 + N_0 E_0) k_1 + (L_0 N_0 - M_0^2) = 0,$$

$$(k_1, k_2) = \left( B \pm \sqrt{B^2 - 4AC} \right) / (2A),$$

$$A = E_0 G_0 - F_0^2, B = L_0 G_0 - 2M_0 F_0 + N_0 E_0, C = L_0 N_0 - M_0^2.$$  \hspace{1cm} (10)

In the thin plate model, the first-order partial derivative can be omitted and thus $E_0 = F_0 = G_0 = L_0 = M_0 = N_0$ and $k_n$ can be described as:

$$E_0 = 1; \quad F_0 = 0; \quad G_0 = 1$$

$$L_0 = \frac{\partial^2 w}{\partial x^2}; \quad M_0 = \frac{\partial^2 w}{\partial x \partial y}; \quad N_0 = \frac{\partial^2 w}{\partial y^2}$$

$$L_0 = \frac{\partial^2 w}{\partial x^2}; \quad M_0 = \frac{\partial^2 w}{\partial x \partial y}; \quad N_0 = \frac{\partial^2 w}{\partial y^2}$$

$$\frac{\partial^2 w}{\partial x^2}; \quad \frac{\partial^2 w}{\partial x \partial y}; \quad \frac{\partial^2 w}{\partial y^2}$$

where $k_1$, $k_2$, and $k_3$ represent the second partial derivatives of the flexure of subducting plate. The maximum ($k_1$) and minimum ($k_2$) curvatures are given as:

$$\langle k_1, k_2 \rangle = \frac{1}{2} (k_1 + k_2) \pm \sqrt{\frac{1}{4} (k_1 - k_2)^2 + k_3^2}$$

(12)

All definitions of symbols used in the calculation of plate maximum curvature are displayed in the Table 2.

3. Results

3.1. 3-D flexural bending and curvature

The flexural bending deformation (Fig. 3) was obtained by comparison with the observed non-isostatic topography of the Mariana Trench (Zhang et al., 2013) (Fig. S1b). The overall deformation pattern

Table 2 Illustration of symbols in calculation of plate maximum curvature (Section 2.3)

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_0$</td>
<td>The coefficient of the first term in the first fundamental formula of the plane</td>
</tr>
<tr>
<td>$F_0$</td>
<td>The coefficient of the second term in the first fundamental formula of the plane</td>
</tr>
<tr>
<td>$G_0$</td>
<td>The coefficient of the third term in the first fundamental formula of the plane</td>
</tr>
<tr>
<td>$L_0$</td>
<td>The coefficient of the first term in the second fundamental formula of the plane</td>
</tr>
<tr>
<td>$M_0$</td>
<td>The coefficient of the second term in the second fundamental formula of the plane</td>
</tr>
<tr>
<td>$N_0$</td>
<td>The coefficient of the third term in the second fundamental formula of the plane</td>
</tr>
<tr>
<td>$k_n$</td>
<td>Normal curvature of the plane</td>
</tr>
<tr>
<td>$k_1$</td>
<td>The maximum curvature of the plane</td>
</tr>
<tr>
<td>$k_2$</td>
<td>The minimum curvature of the plane</td>
</tr>
</tbody>
</table>
is also consistent with the variation in the free-air gravity anomaly (Sandwell et al., 2014) (Fig. S1c). The modeled trench relief $W_0$ ranges from 2.4 to 6.2 km along the trench axis, with RMS value of ~164 m between the model and observation along the trench axis (Fig. 4a and Table S1 in the Supplementary material). The calculated $W_0$ shows an increase in the deformation toward the Challenger Deep (at along-trench distance of 0–300 km) and then a northward decrease in the deformation (at along-trench distance of 300–2,300 km) (Figs. 3 and 4a). The calculated trench width ($X_0$, Fig. 2) also varied significantly, ranging from 36 to 86 km (Table S1 in the Supplementary material). The maximum flexural bending curvature of the subducting Pacific plate was largest near the trench axis and decreased away from the trench axis. The maximum curvature at the trench axis ($K_0$) varied between 0.12 and 1.46 $\times$ 10$^{-6}$ m$^{-1}$ (Figs. 4b and 5a). The southern Mariana Trench had relatively large values of $K_0$ (Fig. 4b), indicating relatively strong flexural bending in comparison to the northern and central Mariana Trench (Figs. 4a).

3.2. 3-D stress distribution and failure zone

We calculated the 3-D deviatoric stress and corresponding yield zone along the Mariana Trench (Table S1 in the Supplementary material). The maximum extensional deviatoric stresses were found in the trench axis of the Challenger Deep ($\sigma_{xx-e}$ = 505 MPa), together with the maximum depth of the extensional yield zone ($D_{xx}$ = 20.4 km) (Table S1). The maximum extensional deviatoric stresses ($\sigma_{xx-e}$) at the trench axis were 395–505 MPa (Table S1 in the Supplementary material) and at depths ($D_{xx}$) of 16.6–20.4 km (Figs. 4c and 5b, Table S1 in the Supplementary material). The bending curvature decreases to a negligible value (0.1 $\times$ 10$^{-6}$ m$^{-1}$) at a characteristic distance ($X_0$) of 116–146 km, which was defined as the yield zone width (Figs. 4d, Table S1 in the Supplementary material). A similar trend was found in the observed width of the visible surface normal faults from the analysis of the multi-beam bathymetry data (Fig. 5c). The corresponding total yield zone area ($S_{yz}$) was in the range of 1,587–2,298 km$^2$ (Fig. 4e and Table S1 in the Supplementary material), which we interpreted as the size of the potential serpentinization zone. The size of the potential serpentinization zone of the southern Mariana Trench was found to be ~1.3 times that of the northern Mariana Trench (Fig. 4e).

4. Discussion

4.1. 3-D effects on plate bending

We identified three types of 3-D effects on plate bending, which were little investigated in previous 2-D studies (Figs. S3 and S4 in the Supplementary material). First, because the 2-D model fails to consider the lateral effect of plate deflection and the direction the 2-D profile may not reflect the bending direction of the plate, the 2-D solutions underestimate the yield zone depth ($D_{xx}$) by up to ~30% for the geometry studied (Figs. S3d and S4d in the Supplementary material). Second, the equation of 2-D elastic model implies a assumption that loads keep constant along the strike of trench. 3-D model can better illustrate the reality by considering the along-strike loading. Third, in the 3-D model, loading at a given point at the trench axis (Fig. S4a in the Supplementary material) can influence deformation within an along-axis distance of $L_i$ (Figs. S5b–d in the Supplementary material). Such a 3-D influence distance ($L_i$) is found to increase with the $T_e$ (Fig. S4e in the Supplementary material). Our calculated yield zones from our 3-D elastic models are close to that of the 2-D elasto-plastic models (Zhou et al., 2018) (Fig. S5 in the Supplementary material). Along the Mariana trench, the $T_e$ at the trench axis ranges in 18-40 km (Zhou et al., 2018), corresponding to the lateral 3-D influence distance of ~95-270 km (Fig. S4e in the Supplementary material).

We built a test model to illustrate the difference on estimating bending stress between 2-D and 3-D model under along-strike variable loading ($V_0$) (Fig. S6 in the Supplementary material). In the test model, $V_0$ changes from $V_0^1$ to $V_0^5$ linearly within a distance $L$ along strike, and the $T_e$ is set to a constant value (35 km) (Fig. S6a in the Supplementary material). We carry out 21 different calculation models in which the ratio $V_0^1$/$V_0^1$ and $L$/$L$ are set to different values (every red dot in Fig. S6d represents one model). We then find that the changes in both $V_0$ and the variation distance $L$ (we used $L$/$L_m$ in Fig. S6d, where $L_m$ is the width of our model) can affect the results (in which the bending stress increases with $V_0$ and decreases with $L$ (Fig. S6d in the Supplementary material).

Seismologists are concerned about the effect of material parameters (such as the Young’s modulus: $E$) on plate on plate deformation. We designed a model to investigate the impact of $E$ on plate deflection and bending elastic stress (Fig. S7). It shows that with increase of $E$, the plate...
deflection becomes smaller while the maximum of bending stress become larger (Fig. S7a). The variation rates of both plate deflection and maximum of bending stress decreases with E (Fig. S7b). This means that for a subducting plate, larger E may causes a deeper area where bending-related normal earthquakes occur.

4.2. Comparison with observed faults, earthquakes, and seismic profiles

We compared the calculated width of yield zone ($X_{yz}$) (Fig. 4d) and the observed surface normal faults (Fig. 5c). Some of normal faults at the outer-rise might not be shown in the bathymetry data because they are too small. Overall, the measured width of the visible surface normal faults is smaller than the calculated $X_{yz}$. Nevertheless, the along-trench variation in the $X_{yz}$ (Fig. 4d) corresponds relatively well with the width of the measured visible surface normal faults (Fig. 5c). The calculated depth of the brittle yield zone was also comparable with the observed seismicity data (Fig. 4c). A total of 66 $M_w \geq 4.0$ normal faulting earthquakes (-135$^\circ$ < rake < -45$^\circ$) during 1976-2020 were located in the outer-rise region of the Mariana Trench (GCMT, http://www.globalcmt.org). Most of these normal faulting events have strikes that were sub-parallel to the trench axis, within 150 km from the trench axis (Fig. 5b), and at a depth of 10–33 km (Fig. 4c). Nighty-five percent (63 out of 66) of the normal faulting earthquakes occurred within the calculated 3-D brittle yield zone (Figs. 4c, 5b, and 6). Most of the relocated normal faulting earthquakes by Eimer et al. (2014) were also within the calculated brittle yield zone (Figs. 4c and 6). Our results overall match the depths of outer rise earthquakes from GCMT and Eimer et al. (2014). Eimer et al. (2020) showed that extensional earthquake occurs to depth of 31km below the seafloor, which is deeper than our results. This may be correlated with the regional stress which is not considered in this study, as outer-rise stress environment depends not only on the plate bending, but also on locking and unlocking of the interplate. Therefore, we suggest that the regional stress (such as frictional resistance on the interplate fault) should be considered in the further works. Furthermore, the calculated yield zone shape also matches relatively well with the shear-wave seismic velocity contour of 3.9 km/s ($V_s$) (Cai et al., 2018), which was suggested to correspond to the boundary of a partial serpentinization zone in the mantle (Figs. 5b and 7).

4.3. Water flux estimation

The bending-induced normal faults provide significant pathways for water to enter the crust and uppermost mantle, enhancing partial serpentinization of the subducting slab. A portion of the water contained in the sediment and oceanic crust is released at shallow depth, whereas the amount of water carried into the deeper mantle can be estimated by the amount of mantle serpentinization of the subducting plate (Emry et al., 2014). Previous studies have estimated the downgoing water flux of the global subduction zones by considering the serpentinized mantle as a homogeneous layer with different subduction rate, such as 4.7cm/yr (Jarrard, 2003), 4.1 cm/yr (Hacker, 2008) and 5.0 cm/yr (Van Keken et al., 2011). Along the southern Mariana Trench, Van Keken et al. (2011) estimated 21.2 Tg/Myr/m for partial serpentinization of the upper 2 km of the mantle. Emry et al. (2014) calculated ~15–30 Tg/Mry/m of downgoing water flux along the southern-central Mariana Trench at ~15°–20°N, assuming the depth of the extensional earthquakes in the outer-rise region corresponded to the depth of the mantle serpentinization. At the northern Mariana Trench, Van Keken et al. (2011) estimated 6.5 Tg/Myr/m for partial serpentinization (Fig. 4f).

In our model, the maximum depth of the yield zone varied in the range of ~16–20 km with an average depth of ~18.5–19.5 km from the northern to southern Mariana Trench (Fig. 4c). Along the Mariana Trench, the subducting crust has an average thickness of ~6–7 km (Van Keken et al., 2011). Therefore, the average depth of the mantle serpentinization below the Moho was estimated to be in the range of ~8–13 km. Following the same assumption of moderate hydration of the upper mantle as in previous studies (Van Keken et al., 2011; Emry et al., 2014), we assumed the degree of the partial serpentinization to be in the range of 1.5–2 wt% H2O, and calculated the average water flux using the mean $D_x$ minus the mean crustal thickness. The resulting average water flux in the southern Mariana Trench was ~34.5–44 Tg/Myr/m, which is about 15% greater than that of the northern Mariana Trench (~28–38.8 Tg/Myr/m).
Myr/m) (Fig. 4f, Table 3). Our results are very close to that of Emry et al. (2014) and about ~2–2.5 times that of Van Keken et al. (2011) (Fig. 4f, Table 3). In the central Mariana Trench at 16°–18°N, our estimation of 31–42 Tg/Myr/m is nearly half of that of Cai et al. (2018) (~79±17 Tg/Myr/m). The difference may come from the fact that Cai et al. (2018) assumed a 24 km thick partially serpentinized layer with 2 wt% water, which is interpreted as area of partial serpentinization in the mantle and pore-water infiltration in the crust.

### 5. Conclusions

By analyzing the plate deflection, stresses, and brittle failure of the subducting plate along the Mariana trench, we draw the following conclusions:

1. The depth of the calculated yield zone varies in the range of ~16–20 km from the northern to southern Mariana Trench. The corresponding water flux in the southern Mariana Trench is estimated to be about 15% greater than that of the northern Mariana Trench.
2. When plate deflection varies along the strike of trench, 3-D effect plays an important role in estimating the trench-axis loading, plate bending stress and yield zone. The difference between 3-D and 2-D result can reach ~30%.
3. The calculated yield zone is consistent with the observed surface normal faults, extensional earthquakes, and the inferred hydration of the subducting plate constrained by seismic velocity anomalies.

### Table 3

<table>
<thead>
<tr>
<th>Along-trench distance (km)</th>
<th>Water flux from Max. $D_{yz}$ (Tg/Myr/m)</th>
<th>Water flux from mean $D_{yz}$ (Tg/Myr/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0-500</td>
<td>58.6±1.8</td>
<td>44.6±1.4</td>
</tr>
<tr>
<td>500-1,000</td>
<td>57.3±0.4</td>
<td>41.8±1.4</td>
</tr>
<tr>
<td>1,000-1,500</td>
<td>55.2±1.0</td>
<td>38.8±1.3</td>
</tr>
<tr>
<td>1,500-2,000</td>
<td>51.3±1.8</td>
<td>34.8±1.3</td>
</tr>
<tr>
<td>2,000-2,500</td>
<td>45.0±3.3</td>
<td>30.2±2.5</td>
</tr>
</tbody>
</table>

- Water flux from Max. $D_{yz}$ means the water flux estimated by the maximum yield zone depth ($D_{yz}$).
- Water flux from mean $D_{yz}$ means the water flux estimated by the mean yield zone depth ($D_{yz}$).

### Declaration of Competing Interest

None.

### Acknowledgements

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### Appendix A. Supplementary data

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### References


